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Note: Concurrently with the 2002–2003 course Ph136, we are producing a final revision of this book. The following table of contents is for the 2000–2001 version of the book, which is available on the Web at

<http://www.pma.caltech.edu/Courses/ph136/ph136.html>

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